

## STUDY OF THE DEFORMATION AND FRACTURE OF ZIRCONIUM ALLOYS UNDER DYNAMIC LOADING

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**Abstract.** The main objective of the present work is the experimental and theoretical investigation of the mechanical properties of the zirconium alloys E110 and E635 in a wide range of strain rates ( $10^{-4} \div 3 \cdot 10^3 \text{ c}^{-1}$ ) and at different temperatures ( $20^\circ\text{C} \div 350^\circ\text{C}$ ). The strain rate and temperature dependencies of deformation diagrams and strength characteristics under tension and compression have been received using the experimental study. The investigated materials have shown sensitivity to strain rate and temperature. Experimental data have been used to identify some LS-DYNA's material models.

**Keywords:** experimental investigation, strain rate, model, nuclear energy, dynamics, temperature, flow stress, plastic strain, ultimate strain

### 1. Introduction

The nuclear industry and energy have special requirements for the materials used. Conventional steels do not pass on safety indicators. Special alloys based on zirconium (Zr) have been developed for this industry. Zirconium is one of the key structural metals in nuclear energy; it is the main component of the alloys used to make the shell of the fuel elements of nuclear reactors. Zirconium alloys have a fairly high corrosion resistance with respect to water and steam and a relatively small cross-section for absorption of thermal neutrons. These alloys favorably differ from pure zirconium in the best mechanical properties. For example, alloy E110 is used as a structural material for the components of the fuel assembly. Currently, this material is the main material for the casings of the fuel rods, spacing grids, and in some cases the guide channels, for PWR (Pressurized water reactor) type reactors. Preservation of high ductility by E110 alloy in combination with corrosion resistance ensures the fuel assemblies' operability to high burnup.

In the new generation reactors, it is assumed that conditions will cause higher stresses in the shells and more intense oxidation processes. In this regard, it is relevant to search for alternative alloys not only for the casings of fuel elements, but also for structural elements of a fuel assembly, such as guide channels, a central pipe, and corners of a rigid frame capable of providing the required fuel resource.

Recently, a multicomponent alloy E635 has been widely used as a material for fuel assemblies of the water-moderated reactor with a capacity of 1000 MW.

During the transport and technological operations such as fuel movement, loading/unloading of fuel, situations may arise that are accompanied by dynamic influences. To obtain reliable estimates of numerical modeling, it is necessary to use deformation models and strength criteria corresponding to the problem being solved. In dynamics problems, it is important to take into account the strain rate influence on the material characteristics. Extensive experimental research is required to build mathematical models describing this effect.

Despite the widespread use of zirconium alloys in nuclear power engineering, as well as the importance of studying the dynamic properties of alloys based on zirconium, there are very little data on this. Investigations of the mechanical characteristics of the metal alloy E110 were carried out in [1]. In this study, the behavior of a zirconium alloy was studied under shock-wave loading conditions. The authors determined the spall strength at strain rates of  $10^5$ - $10^6$  s<sup>-1</sup> using laser interferometers VISAR and POV. At shock compression pressures of above 10.6 GPa it was obtained a three-wave structure of the compression pulse. According to the authors, this effect is associated with polymorphic transformations  $\alpha$ - $\omega$ . In [2] the dynamic characteristics of the MA-15-Ti magnesium alloy were determined using the Kolsky method. Zirconium is a structure modifier in this alloy and it significantly improves physical and mechanical properties. There are few studies [3-7], which are devoted to the study of the dynamic mechanical properties and microstructural features of deformation in the adiabatic shear bands of amorphous zirconium-based alloys at strain rates about  $10^3$  s<sup>-1</sup>. For the investigated alloys an increase in the strength characteristics with increasing strain rate is noted, microstructural features of deformation are revealed and the mechanisms of formation of adiabatic shear bands are studied. In [8-13] the dynamic properties of ceramics based on zirconium are investigated using the Kolsky method and its modifications. Dynamic diagrams of deformation under a uniaxial stress state, as well as strength and deformation properties under uniaxial strain, were obtained.

The present work is devoted to the determination of the strain rate and temperature dependences of the deformation curves and ultimate plasticity characteristics of E110 and E635 zirconium alloys.

## 2. Test specimens

Specimens of two zirconium alloys E110 and E635 were subjected to quasistatic and dynamic tests. The chemical composition of these alloys is given in Table 1.

Table 1. The chemical composition of tested alloys

Denotation	Mass content, %					
	Zr	Nb	Sn	Fe	O	impurities
E110	Base	0.9-1.1	-	0.05	0.1	0.18
E635	Base	0.9-1.1	1.1-1.5	0.3-0.5	0.1	0.15

The compression test specimens were in the form of cylinders with dimensions  $\varnothing = 16$  mm  $L_0 = 8$  mm for static tests and  $\varnothing = 10$  mm  $L_0 = 5$  mm for dynamic tests. For tensile tests, samples with threaded heads had the dimensions of the working part:  $\varnothing = 5$  mm,  $L_0 = 15$  mm for static tests and  $\varnothing = 5$  mm,  $L_0 = 10$  mm for dynamic tests.

## 3. Test methods

Static compression and tensile tests of the specimens at temperatures of + 20°C and + 350°C were carried out on a ZwickRoell Kappa 50 DS experimental setup with a maximum loading force of  $\pm 600$  kN. The measuring equipment included a class 1 force sensor in accordance with ISO 7500-1 and a high-precision displacement meter built into the movable beam of the

90 A.I. Romanov, V.A. Panov, M.A. Samsonov, D.E. Chirkin, A.M. Bragov, L.A. Igumnov, A.Yu. Konstantinov, A.K. Lomunov machine, with an accuracy of positioning of the beam in a predetermined position of not more than  $\pm 2 \mu\text{m}$ . To obtain the elastic modulus  $E$  of the materials, we used a high-precision high-temperature extensometer RMA-12 / V7-1 (resolution  $0.1 \mu\text{m}$ ) installed on the working part of the sample and allowing to determine the elastic modulus at normal and elevated temperatures. The testing machine is equipped with a MAYTEC-HT 080/1 heating device.

Compression and tensile tests in the dynamic range of strain rates ( $5 \cdot 10^2$ - $5 \cdot 10^3 \text{ s}^{-1}$ ) at temperatures  $+20^\circ\text{C}$ ,  $+200^\circ\text{C}$ , and  $+350^\circ\text{C}$  were carried out using the Kolsky (or Split Hopkinson Pressure Bar) method [14] and its modifications [15-17]. The following formulas can be used to calculate stress, strain, and strain rate in a specimen based on recorded pulses in the measuring bars:

$$\sigma_s(t) = \frac{EA}{2A_s^0} \varepsilon_1(t), \quad (1)$$

$$\varepsilon_s(t) = \frac{C}{L_0} \int_0^t \varepsilon_2(\theta) d\theta, \quad (2)$$

$$\dot{\varepsilon}_s(t) = \frac{C}{L_0} \cdot \varepsilon_2(t). \quad (3)$$

Here  $E$  – elastic modulus of the measuring bar,  $A$  – measuring bar's cross-section area,  $C$  – sound speed in the measuring bar,  $L_0$  and  $A_s^0$  – initial length and initial cross-section area of the specimen.

Instead of the  $\varepsilon_1(t)$  and  $\varepsilon_2(t)$ , one of three expressions can be substituted, respectively:

– for stress calculation:

$$\varepsilon_1(t) = \begin{cases} \varepsilon^I(t) + \varepsilon^R(t) + \varepsilon^T(t) \\ 2 \cdot (\varepsilon^I(t) + \varepsilon^R(t)) \\ 2 \cdot \varepsilon^T(t) \end{cases} \quad (3)$$

– for strain calculation:

$$\varepsilon_2(t) = \begin{cases} \varepsilon^I(t) - \varepsilon^R(t) - \varepsilon^T(t) \\ 2 \cdot (\varepsilon^I(t) - \varepsilon^T(t)) \\ -2 \cdot \varepsilon^R(t) \end{cases} \quad (4)$$

Further, from the obtained parametric dependences  $\sigma_s(t)$ ,  $\varepsilon_s(t)$  and  $\dot{\varepsilon}_s(t)$  time is excluded, and a deformation diagram  $\sigma_s(\varepsilon_s)$  of a specimen with a known dependence  $\dot{\varepsilon}_s(\varepsilon_s)$  is constructed. During the test, using a strain gauge on measuring bars, a loading stress (strain) impulse is recorded. The shape, amplitude, and duration of this impulse are set by choosing the length, material, and velocity of the striker which is accelerated in the barrel of the gas gun. In addition, stress (strain) pulses reflected from the specimen and transmitted through it are recorded, which are the "responses" of the material to the applied load and allow constructing a dynamic diagram of the test specimen.

An experimental setup that implements the SHPB method includes a pneumatic loading device (gas gun with a caliber of 20 mm) with a control system, a complex of measuring and recording equipment, and replaceable sets of bars made of steel or aluminum alloy with a diameter of 20 mm for testing under various conditions. In the present investigation bars made of high-strength steel with a yield strength of about 2000 MPa are used. The bars are fixed and centered in textolite plain bearings, which allow adjustment of their relative position with the help of adjusting elements to ensure alignment of the bars with each other and with the striker. The strain is measured using small-base strain gauges glued to the lateral surface of the bars at a considerable distance from the specimen. Moreover, to compensate for bending vibrations in the bars and increase the amplitude of the useful signal in the working sections, 4 strain gauges connected in series are glued. To study the behavior of materials at elevated temperatures, a miniature tube-type furnace is used. It warms the ends of the measuring bars with a sample located between them. An XC thermocouple welded to the side

surface of the sample was used to control the temperature of the specimen. At test temperatures up to +350°C any correction of the formulas and the method of processing experimental information was not performed, since at such temperatures, there are no noticeable changes in the elastic characteristics of the material of the bars (elastic wave velocity and elastic modulus).

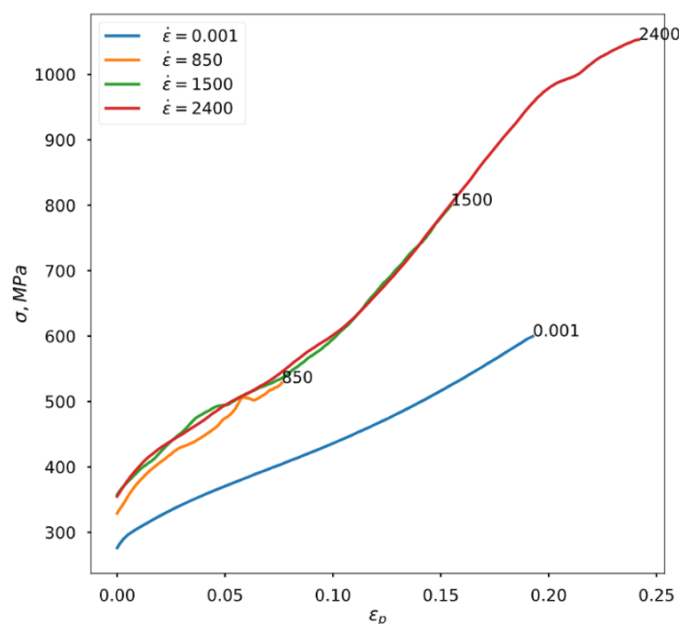
#### 4. Test results

The deformation diagrams at static compression and tension of the E110 and E635 alloys were constructed at temperatures  $T = 20^\circ\text{C}$  and  $350^\circ\text{C}$ . Three samples were tested at each temperature, and the results were averaged.

Dynamic tests at high strain rate tension were carried out using the Nicholas scheme [16]. Four conditions were implemented in terms of strain rate: 1000, 1500, 2000, and  $2800\text{ s}^{-1}$  as well as three conditions in terms of temperature: +20, +200, and +350°C. In each loading condition, five specimens were tested to determine the scatter characteristics of the experimental data.

The compression schemes were used to obtain strain curves. The tensile schemes were used to determine the ultimate fracture characteristics.

Figure 1 illustrates the effect of the strain rate on the strain curves of the E110 alloy. Dynamic curves have larger initial yield strength and the angle of the plastic part of the curve. In the strain rate range from  $850$  to  $2400\text{ s}^{-1}$ , the effect of strain rate hardening is weakly expressed.

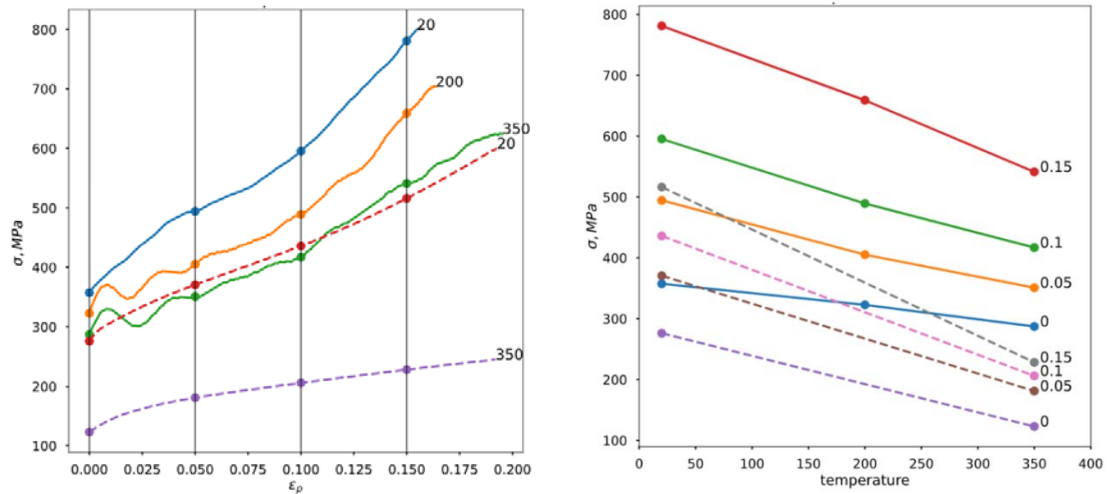


**Fig. 1.** Strain rate influence on strain curves. E110 alloy

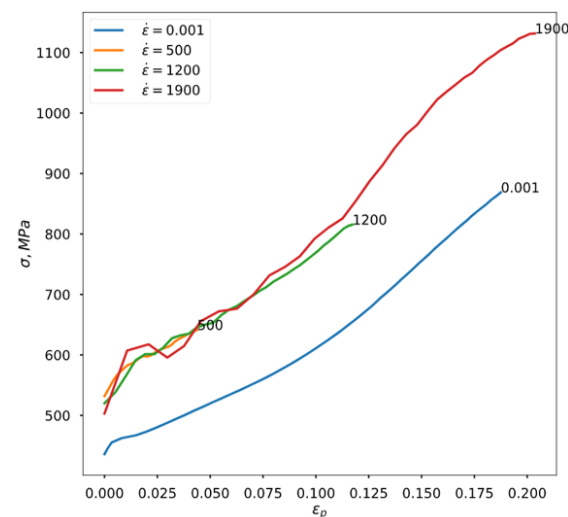
The left side of Fig. 2 illustrates the effect of temperature on the strain curves of E110 alloy. Dashed lines are static curves. The solid lines are the dynamic curves, obtained at strain rate  $\sim 1500\text{ s}^{-1}$ . The corresponding temperatures in Celsius degree are shown next to the each line. The right part of Fig. 2 shows slices of curves at different plastic strain levels (the corresponding plastic strain values are shown next to the each line). Dashed lines are static curves. The solid lines are the dynamic curves. If we analyze the results, it turns out that in the static region the influence of temperature is more pronounced. This can be seen by the slope of the curves on the right part of Fig. 2.

Figure 3 shows the deformation curves of the E635 alloy at different strain rates. It can be noted that this material has a higher resistance to deformation than the E110 alloy.

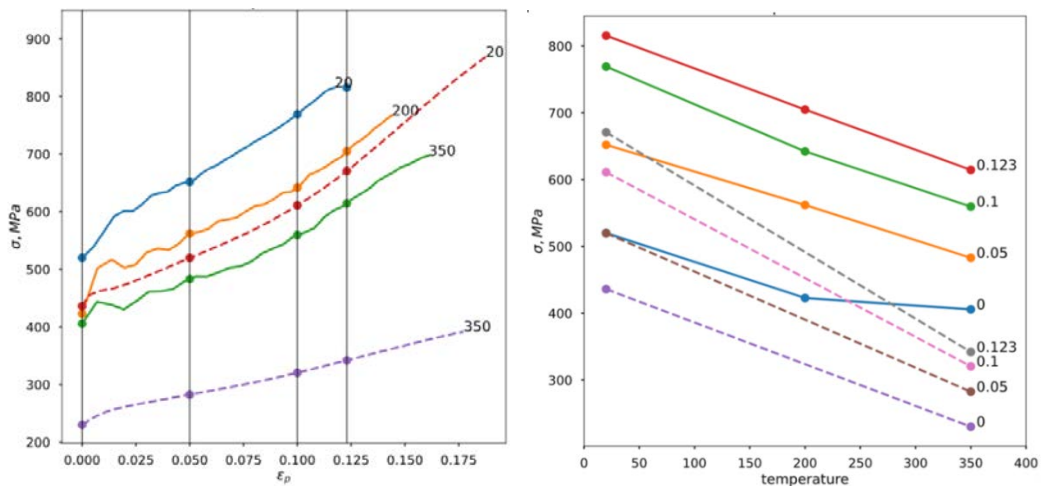
Figure 4 illustrates the effect of temperature on E635. The same effect is observed as in the case of alloy E110.



**Fig. 2.** Temperature influence on strain curves. E110 alloy



**Fig. 3.** Strain rate influence on strain curves. E635 alloy



**Fig. 4.** Temperature influence on strain curves. E635 alloy

Based on the shape of the specimens fractured in tension the ultimate plastic strains were determined using the formula:

$$\varepsilon_p^f = \ln \frac{1}{1 - \frac{D_0^2 - D^2}{D_0^2}}. \quad (5)$$

Here  $D_0$  – initial diameter of the specimen's cross section,  $D$  – diameter of the fractured specimen's cross-section in the neck.

The obtained data will be illustrated in the section «Model identification».

## 5. Model identification

To use in the numerical simulation, the obtained data must be turned into a mathematical model. So, the experimental surfaces were approximated by analytical functions.

The Johnson-Cook model is widely used to describe the dynamic behavior of viscoplastic materials. The mathematical formulation for the dependence of the radius of the yield surface on the strain, strain rate, and the temperature is formulated as follows [18,19]:

$$\sigma = (A + B \cdot \varepsilon_p^n)(1 + C \cdot \ln \dot{\varepsilon}_p^*)(1 - T^{*m}). \quad (6)$$

Here  $T^* = \frac{T - T_0}{T_m - T_0}$ ,  $\varepsilon_p$  – equivalent plastic strain,  $\dot{\varepsilon}_p^* = \dot{\varepsilon}_p / \dot{\varepsilon}_0$  – dimensionless plastic strain rate,  $\dot{\varepsilon}_0 = 1.0 \text{ s}^{-1}$ ,  $T_0$  and  $T_m$  – room (or reference) temperature and melting temperature respectively. Five material constants are determined empirically:  $A$ ,  $B$ ,  $n$ ,  $C$  и  $m$ .

In addition to the classical, linear in the logarithm of strain rate multiplier

$$1 + C \cdot \ln(\dot{\varepsilon}^*), \quad (7)$$

other options exist to take into account the influence of the strain rate on the flow stress:

- model of Huh-Kang [20]:

$$1 + C \cdot \ln(\dot{\varepsilon}^*) + C_2 \cdot \ln(\dot{\varepsilon}^*)^2, \quad (8)$$

- model of Cowper-Symonds [21]:

$$1 + \left(\frac{\dot{\varepsilon}^*}{C}\right)^{\frac{1}{p}}, \quad (9)$$

- model of Allen-Rule-Jones [22]:

$$(\dot{\varepsilon}^*)^C. \quad (10)$$

Approximation independent material characteristics for E110 and E635 alloys are shown in Table 2.

Table 2. E110 and E635 properties

Property	Value	Dimension
Density, $\rho$	6600	kg/m <sup>3</sup>
Young's modulus, E	95	GPa
Poisson's ratio, $\nu$	0.34	
The melting temperature, $T_m$	2106	K
$T_0$	293	K
Specific heat, $c_p$	0.24	kJ/kg/K

The disadvantage of the model is that the various effects are independent of each other. Thus, due to the multiplicative formulation, the temperature softening is the same for statics and dynamics, which does not allow us to describe the effect obtained earlier.

You can either focus on static data and well describe the effect of temperature in statics. In this case, the dynamic curves at different temperatures are poorly described (left side of Fig. 5). On the other hand, we can approximate dynamic curves well and get a poor description of static temperature softening (right side of Fig. 5).

In Figure 5 dotted lines correspond to experimental curves, solid ones – to the mathematical model. Blue color indicates data at room temperature, orange – at temperature 200°C, and red – at temperature 350°C. Parameters of the mathematical model for static and dynamic temperature softening cases are given in Tables 3 and 4.

Table 3. Johnson-Cook parameters. E110, focus on static temperature softening

A	324	MPa
B	3684	MPa
n	1.324	
C	0.032	
m	0.36	

Table 4. Johnson-Cook parameters. E110, focus on dynamic temperature softening

A	325.4	MPa
B	3756	MPa
n	1.34	
C	0.032	
m	0.73	

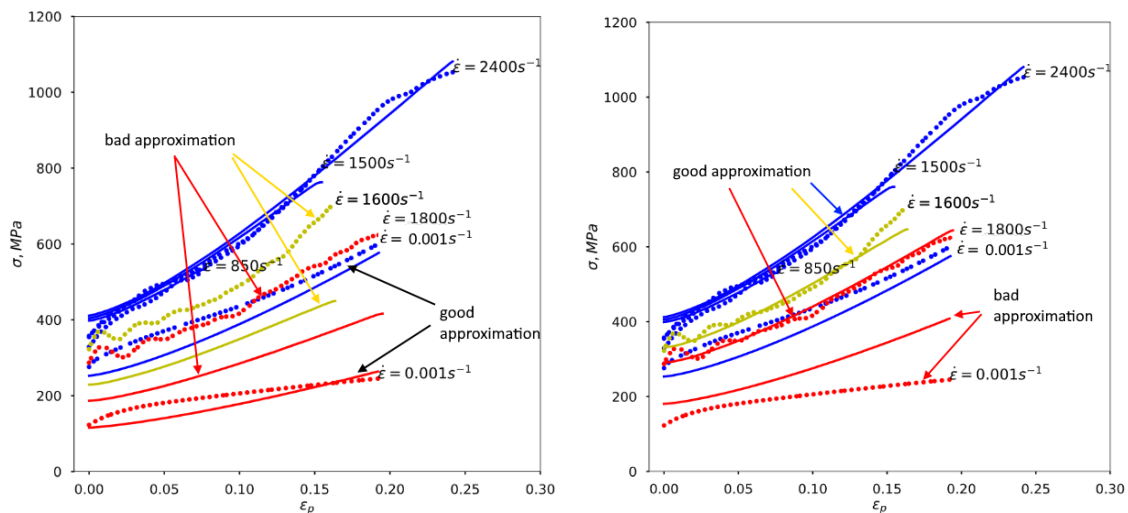


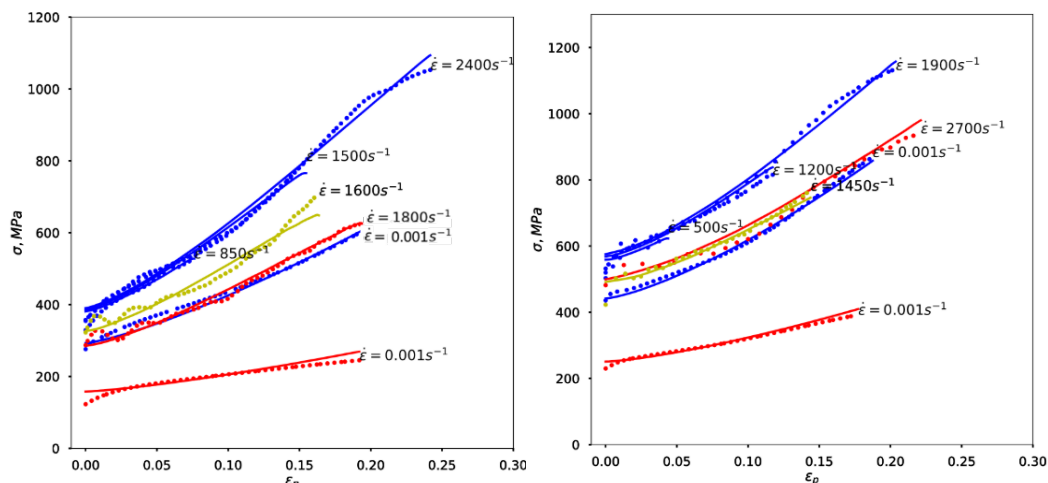
Fig. 5. E110 data approximation by the Johnson-Cook equation

In addition, the modified Johnson-Cook model was considered [6]:

$$\sigma = \sigma_A + B \cdot e^{-(\beta_0 - \beta_1 \ln \dot{\epsilon})T} + A \cdot \epsilon^n \cdot e^{-(\alpha_0 - \alpha_1 \ln \dot{\epsilon})T} \tag{11}$$

Here  $\sigma_A, B, \beta_0, \beta_1, A, n, \alpha_0, \alpha_1$  – model's parameters.

This model has more parameters but allows describing more complex effects. It can be seen from Fig. 6 that this model allowed us to approximate the experimental data with sufficient accuracy. Modified Johnson-Cook parameters for E110 and E635 alloys are shown in Table 5.



**Fig. 6.** Data approximation by the modified Johnson-Cook equation for E110 (left) and E635 (right)

**Table 5.** Modified Johnson-Cook parameters

	E110	E635	
$\sigma_A$	0	0	MPa
$B$	507	730	MPa
$\beta_0$	0.0014	0.0013	
$\beta_1$	$6.4 \cdot 10^{-5}$	$5.9 \cdot 10^{-5}$	
$A$	6512	8956	MPa
$n$	1.3	1.36	
$\alpha_0$	0.0022	0.0022	
$\alpha_1$	0.00013	$6.43 \cdot 10^{-5}$	

The obtained strain rate and temperature dependence of the ultimate plastic strain were approximated by the model:

$$\varepsilon_p^f = D_1 \cdot (1 + \dot{\varepsilon})^{D_4} \cdot \left(1 + D_5 \cdot \frac{T - T_0}{T_m - T_0}\right). \quad (12)$$

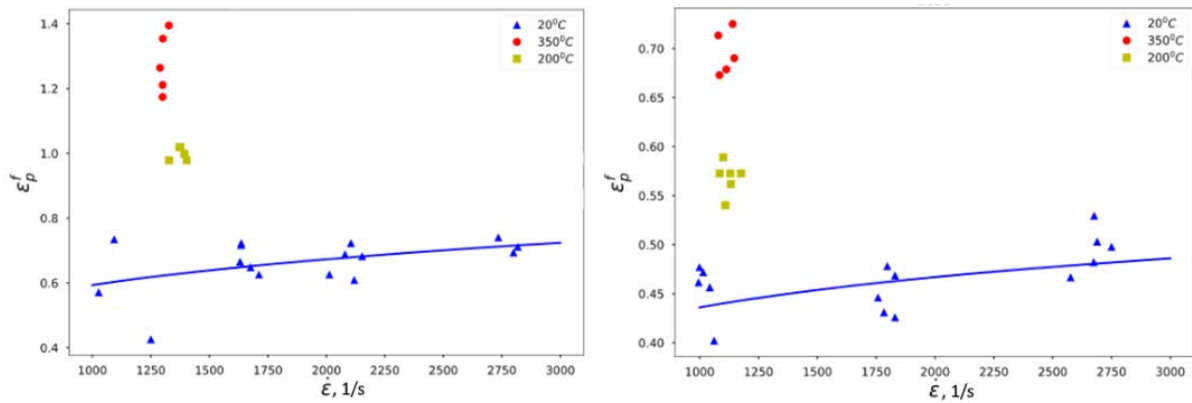
Parameters of approximation are given in Table 6.

**Table 6.** The ultimate plastic strain approximation parameters

	E110	E635
$D_1$	0.17	0.22
$D_4$	0.181	0.1
$D_5$	5.83	3

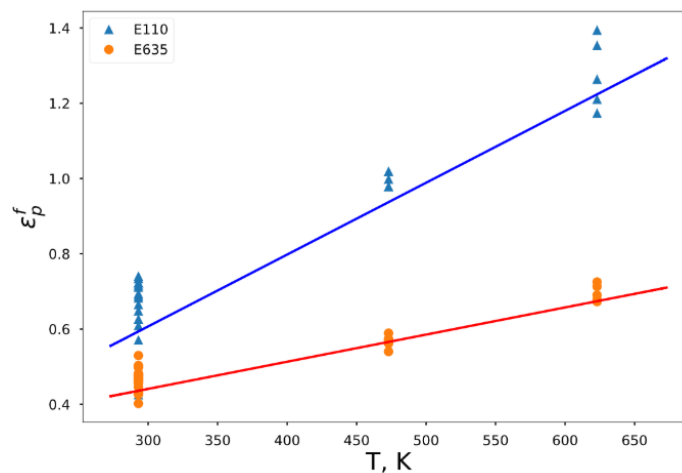
Figure 7 illustrates the dependence of the ultimate plastic strain on strain rate and temperature. Markers correspond to experimental data obtained at different temperatures. The solid line corresponds to the mathematical model. It can be noted that the ultimate strain increases slightly with increasing strain rate and significantly increases with temperature rise.





**Fig. 7.** Ultimate plastic strain for E110 (left) and E635 (right)

Figure 8 illustrates the approximation of the temperature dependences of the fracture strain for the studied alloys. It can be noted that the E635 alloy is fractured at lower values of plastic strain. The temperature has a greater effect on the ultimate characteristics of the E110 alloy.



**Fig. 8.** Temperature dependence of ultimate plastic strain for E110 (left) and E635 (right) and its approximations

## 6. Conclusions

As a result of the investigation of deformation of alloys E110 and E635 under compression and tension in a wide range of strain rates and temperatures from 20°C up to 350°C, mechanical characteristics are obtained in the form of deformation diagrams. It is noted that the mechanical behavior of the investigated alloys is sensitive to the strain rate and temperature. Obtained data is approximated by the modified Johnson-Cook model reasonably well. E635 alloy has a higher resistance to deformation than the E110 alloy but is fractured at lower values of plastic strain. The temperature has a greater effect on the ultimate characteristics of the E110 alloy than on the E635 alloy. As a result of the study, the mathematical models of the deformation and strength criteria are constructed which can be used in the development of digital copies of nuclear engineering designs.

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